

# Transistors Demystified

(HOPEFULLY)

By now, you have seen a very large number of equations describing what you have always been told is a switch,

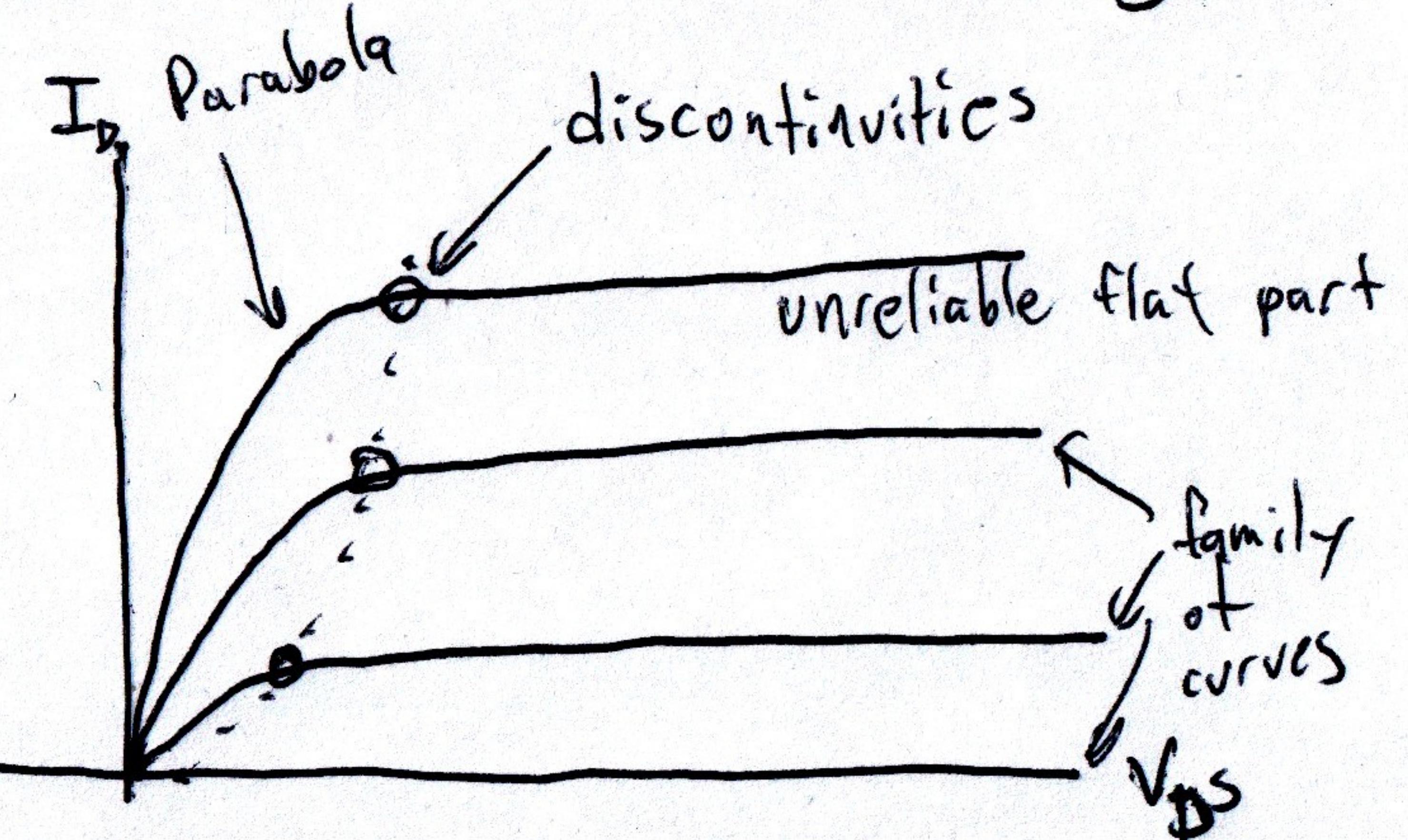
$$I_D = K' \frac{W}{L} \left( V_{GS} - V_{TN} - \frac{V_{DS}}{2} \right) V_{DS}$$

$$K' = \mu_n C_{ox}$$

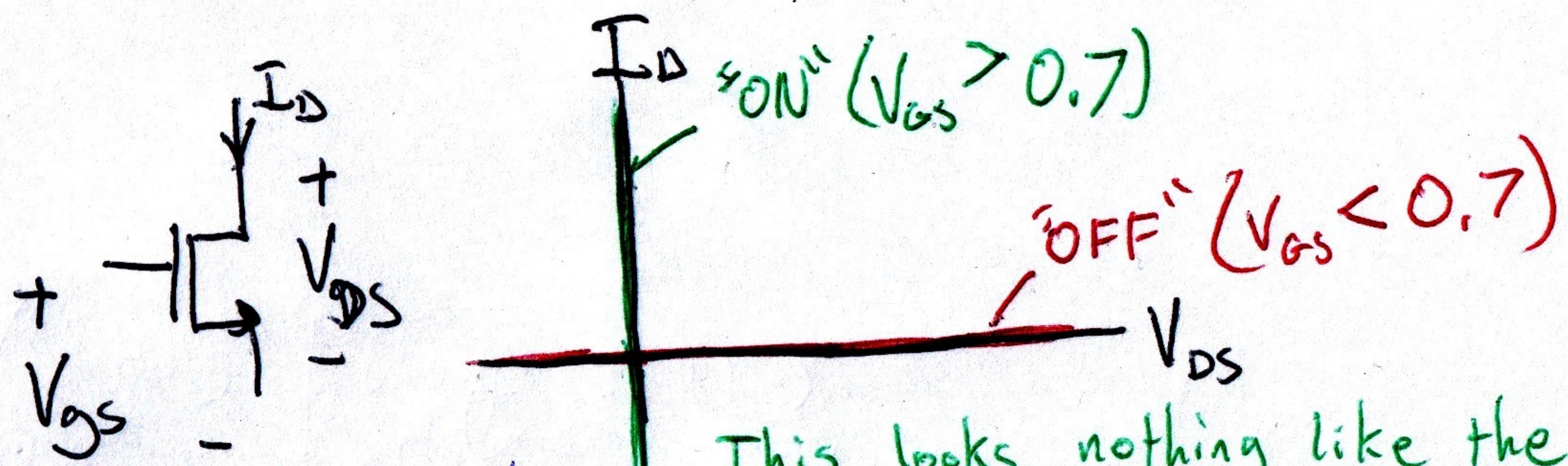
$$V_{DSAT} = V_{GS} - V_{TN}$$

$$C_{ox}'' = \epsilon / K_{ox} \quad V_{TP} = V_{TO} - \gamma / S$$

You have also seen an I-V curve that looks like your AP Calculus teacher's idea of a cruel joke:



So let's back up a bit and look at a transistor as a switch.

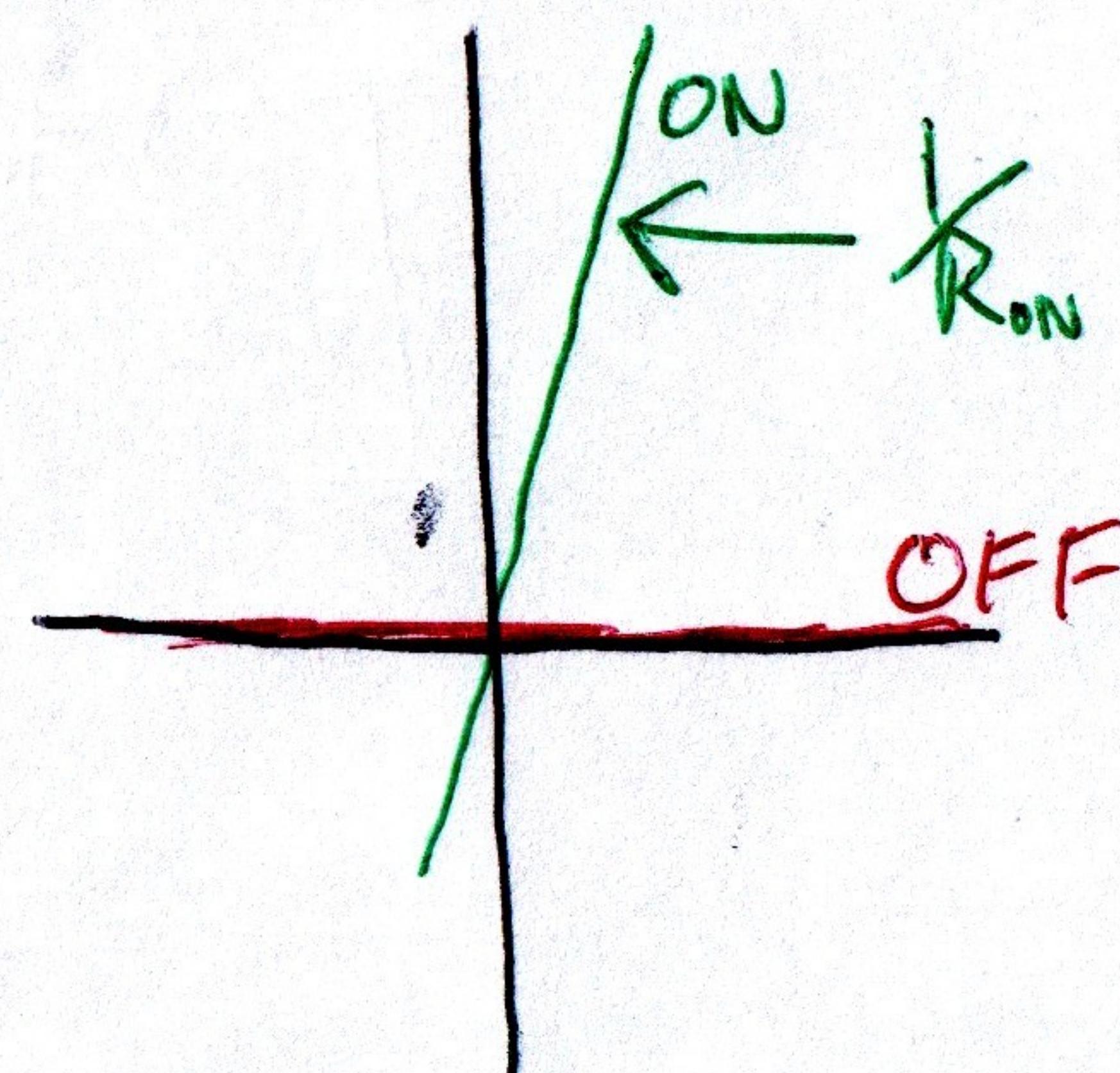


- A horizontal line at  $I=0$  is an open
- A vertical line at  $V=0$  is a short.

This looks nothing like the real curve, but it acts like a true switch.

|                  |
|------------------|
| ON: $V_{DS} = 0$ |
| OFF: $I_o = 0$   |

Believe it or not, this is often a good enough model for basic analysis, although sometimes you may go a little better with a series on resistance:

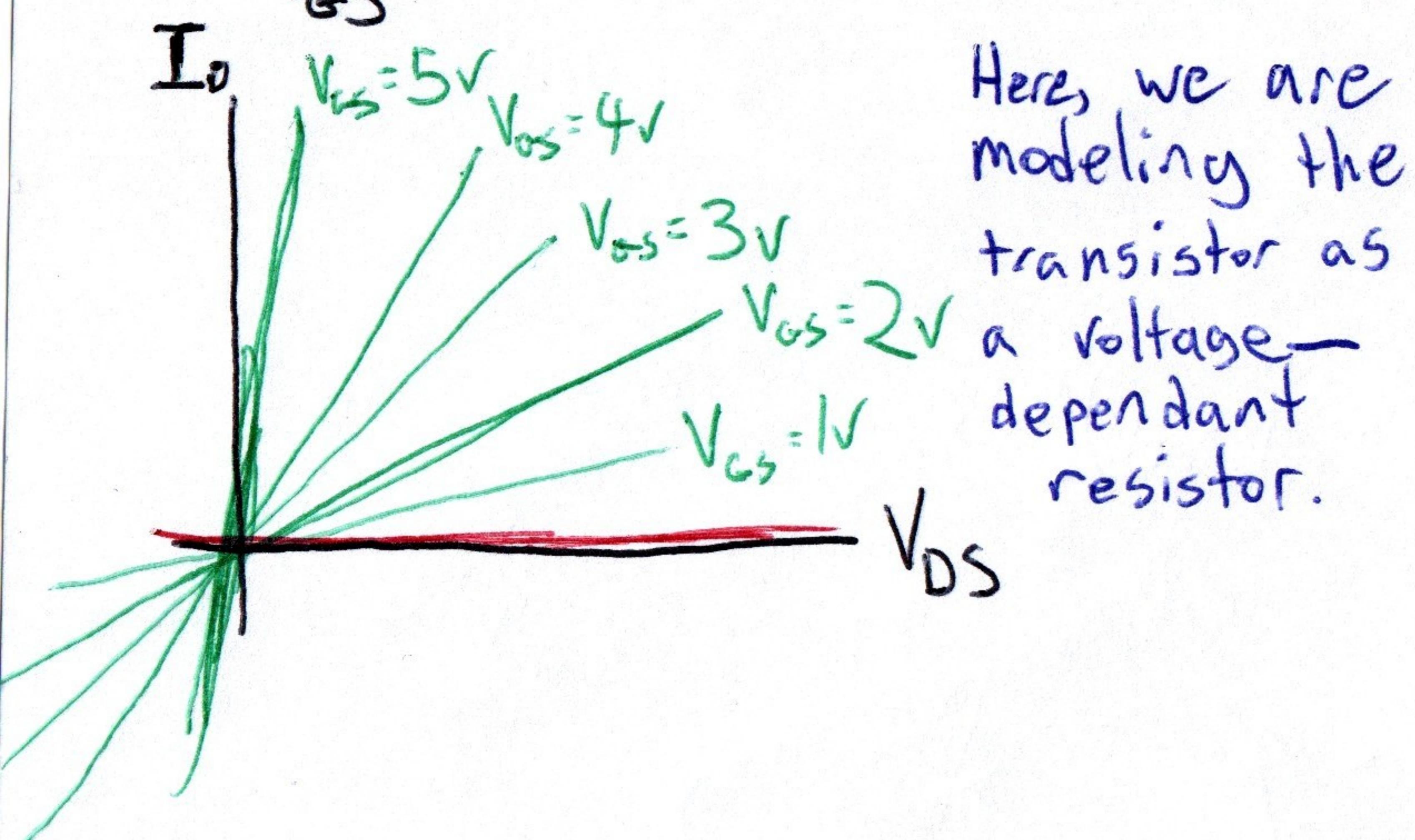


$$R_{ON} = \frac{V_{DS}}{I_D}$$

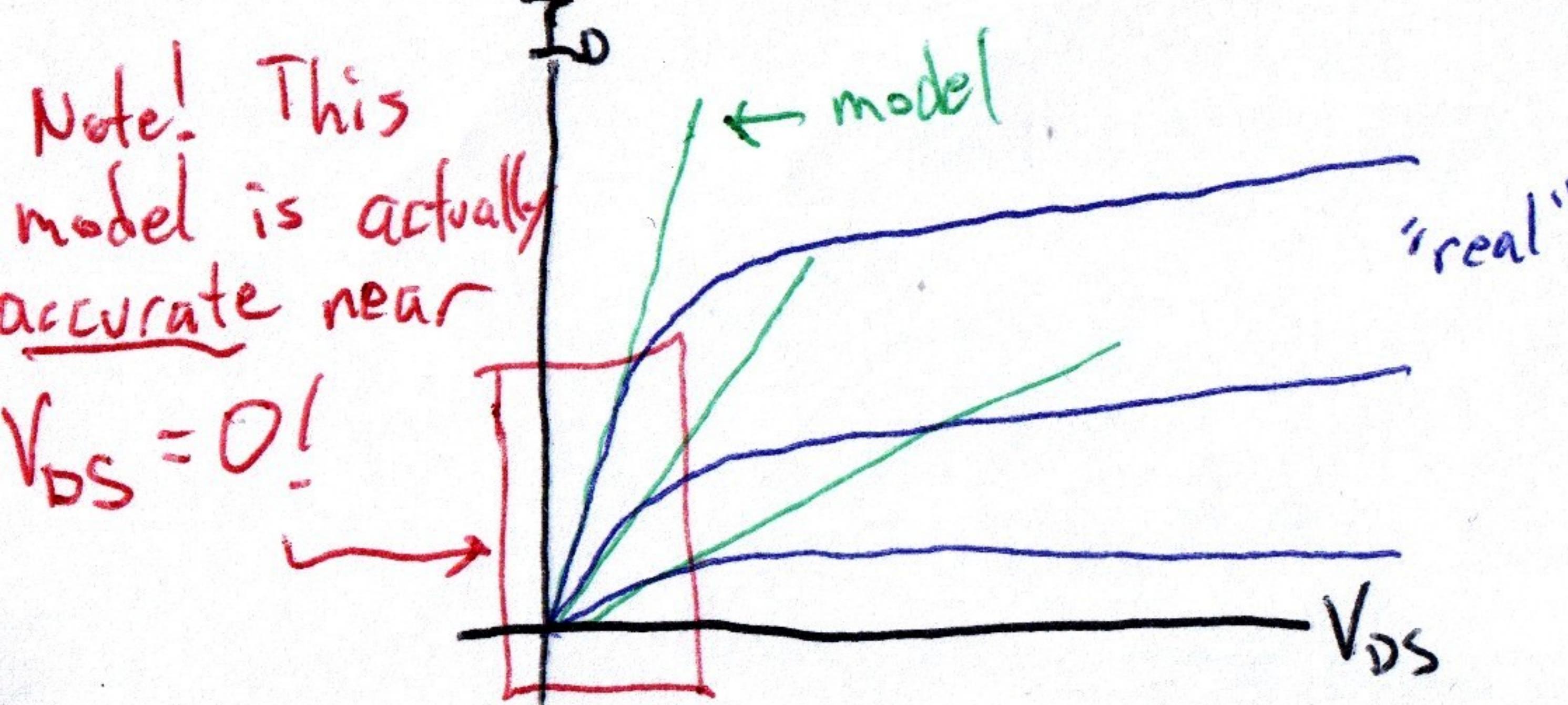
(triode only)

$$= \frac{1}{K' \frac{W}{L} \left( V_{GS} - V_{TN} - \frac{V_{DS}}{2} \right)}$$

Another popular simple model is as a variable resistance, where "R<sub>on</sub>" becomes a variable, dependant on V<sub>GS</sub>:



This is the first time we can see PART of the real IV curves in the model:



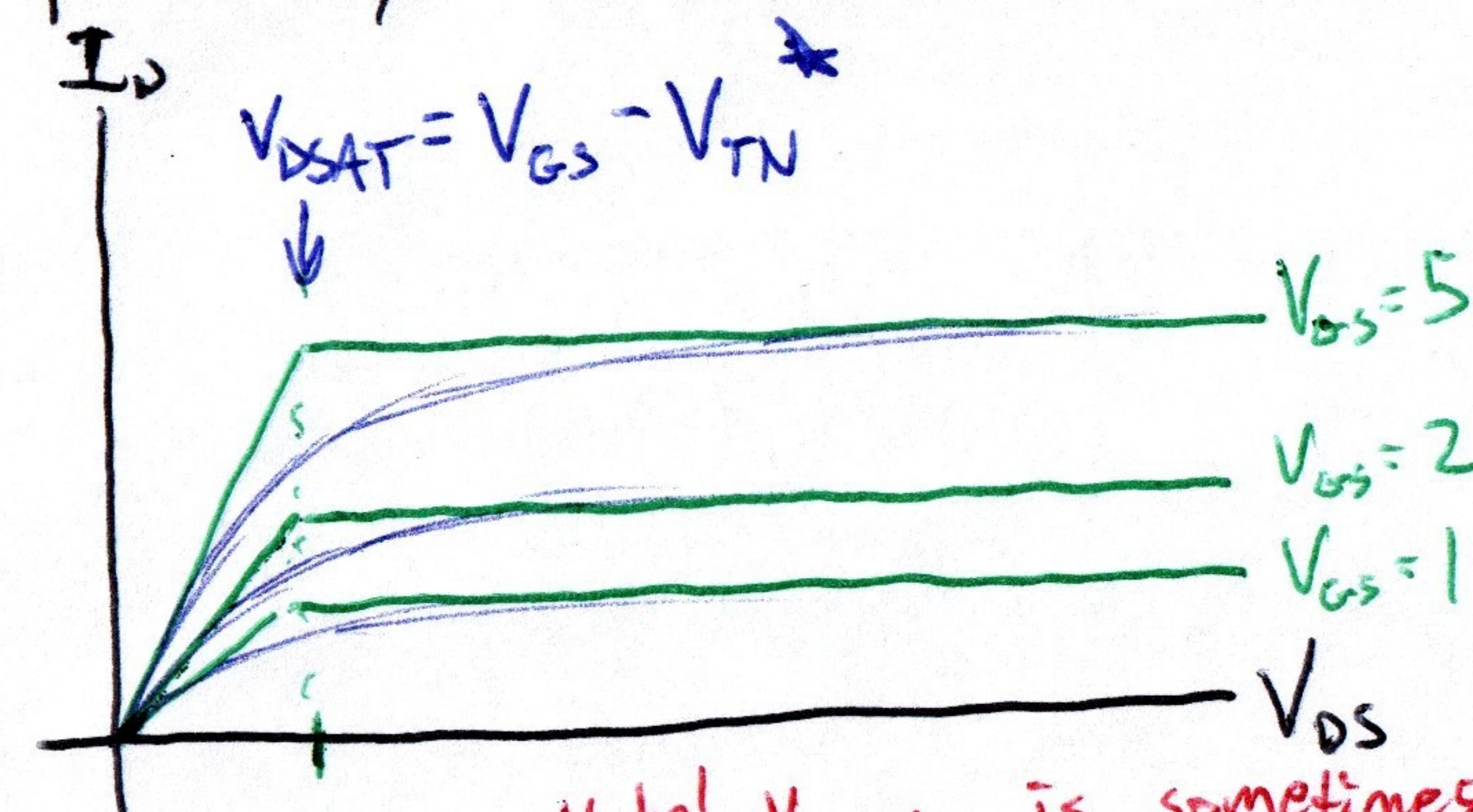
The variable resistance model only gets really bad at high V<sub>DS</sub>, which is to say, saturation. In saturation, I<sub>D</sub> is much more dependent on V<sub>GS</sub> than V<sub>DS</sub>, so the simplified version of this has this as a perfectly horizontal line:

Triode: USE R<sub>ON</sub>

Saturation:

$$I_D = \frac{K_n' W}{2 L} (V_{GS} - V_{TN})^2$$

$$(V_{GS} - V_{TN} \leq V_{DS})$$



Note! V<sub>DSSAT</sub> is sometimes a pretty vague concept, so calculations near V<sub>DSAT</sub> can get ugly!

For digital applications, it's pretty rare to go more complex than this, but in Analog (Amplifiers, etc) more complex models are common.

\*If you're feeling reckless or impatient, you can use the rule of thumb  $V_{DSAT} \approx 0.3$  (Analog engineers do this all the time)

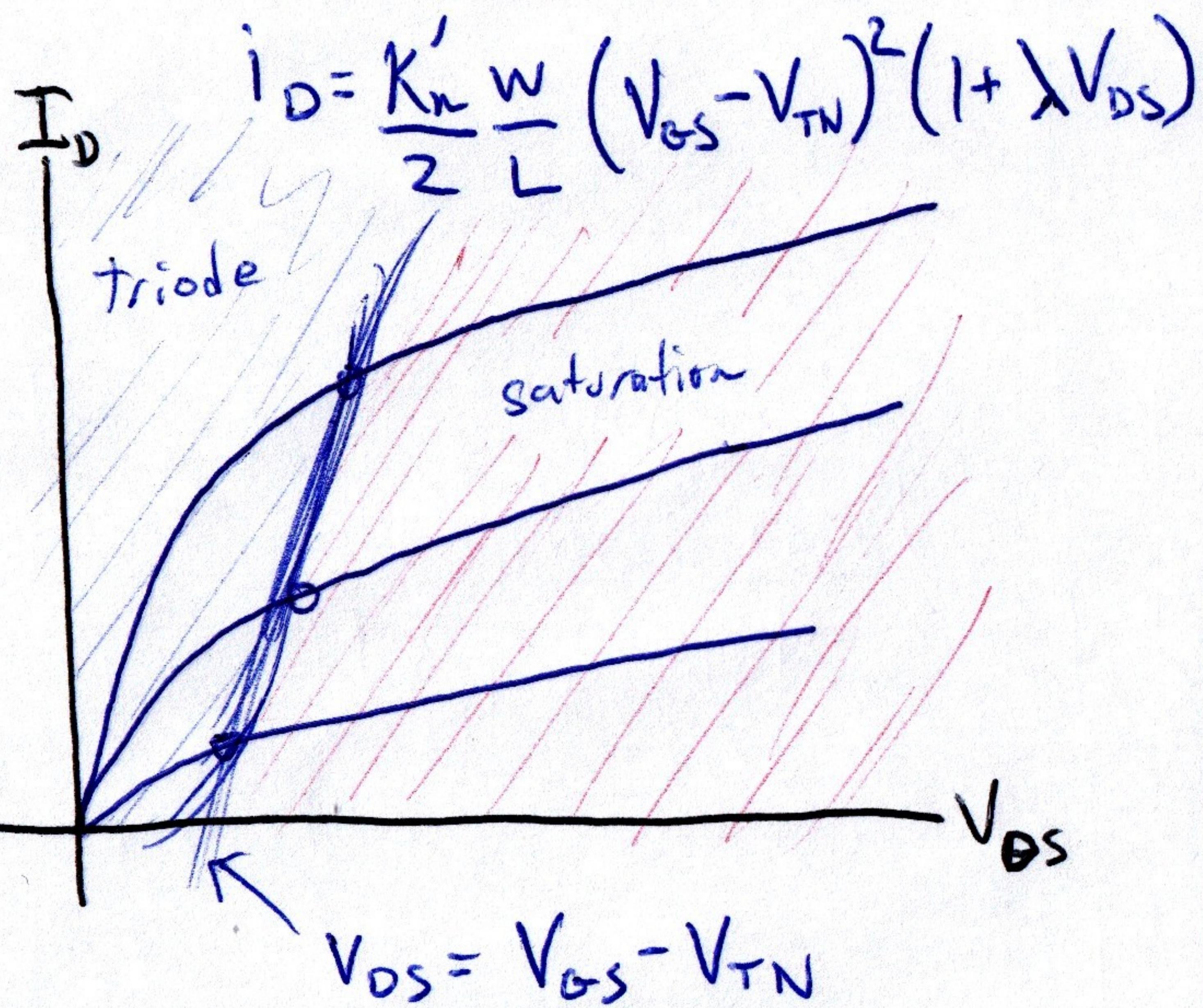
As more detailed calculations pile on, it gets more likely that you should switch to SPICE, but watch out! Even SPICE models have limits, and it is very wrong (although lots of people do it) to say that SPICE is the ultimate authority.

"Full"

NMOS Model:

$$i_D = K_n \frac{W}{L} \left( V_{GS} - V_{TN} - \frac{V_{DS}}{2} \right) V_{DS}$$

OR



(Not Shown, the Body Effect:)

$$V_{TN} = V_{TO} + \gamma \left( \sqrt{V_{SB} + 2\phi_F} - \sqrt{2\phi_F} \right)$$

... or the many, many weird things happening in modern SPICE models...

$$\cancel{V_{th} = V_{th0} + K \left( (\phi_s - V_{DS}) - \sqrt{\phi_s} \right) - K_2 V_{bs} + K_1 \sqrt{\phi_s} \left[ 1 + \frac{N_{eff}}{L_{eff}} - 1 \right]}$$

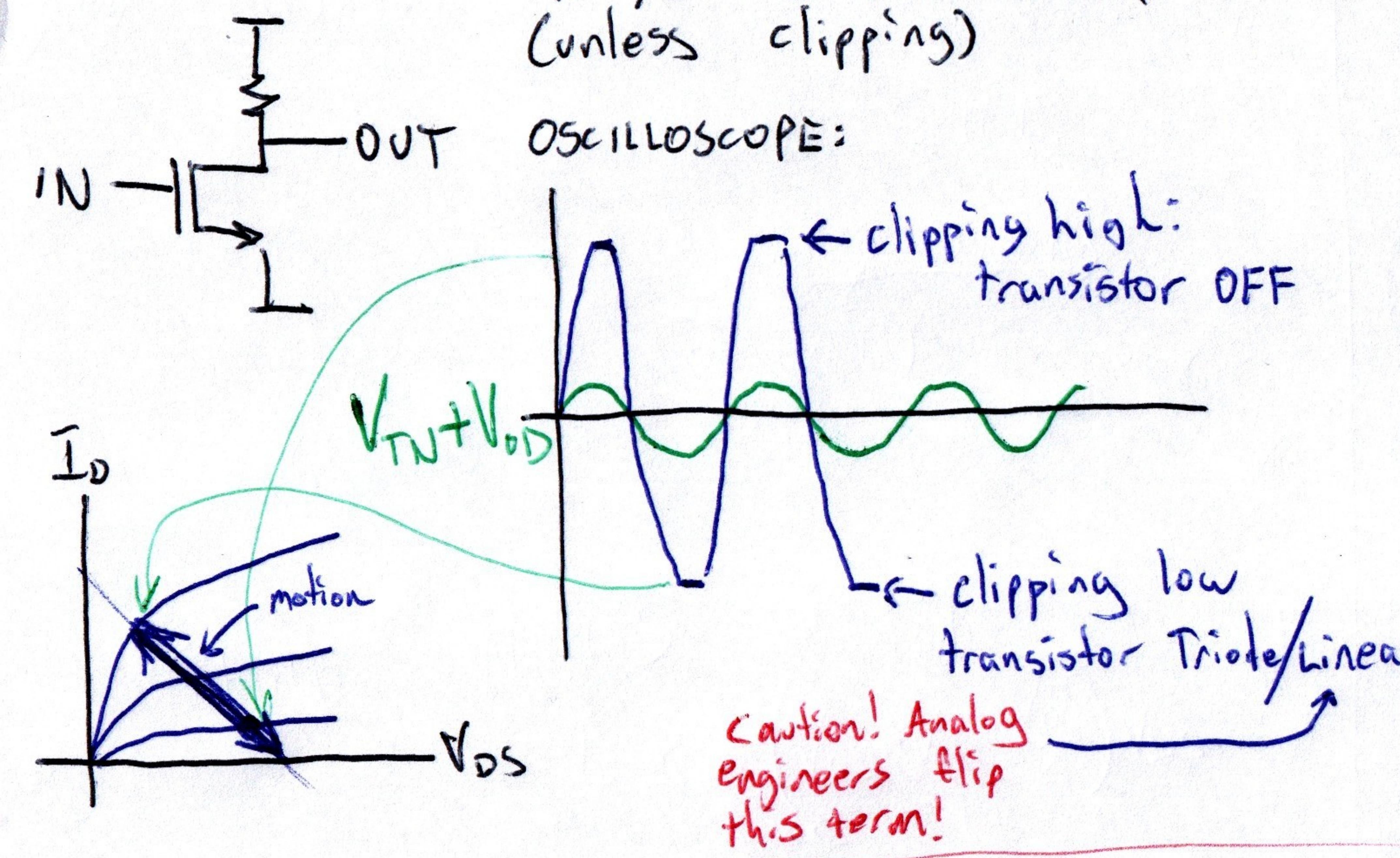
$$\cancel{\frac{\pi q N_a (x_{dmax})^2}{2 C_{ox} W} = 3 \pi \frac{T_{ox}}{W} \phi_s}$$

$$\cancel{I_{DS} = N_{eff} C_{ox} \frac{W}{L} \frac{1}{1 + V_{DS}/E_{sat}} (V_{gs} - V_{sh} - A_{bulk} V_b)}$$

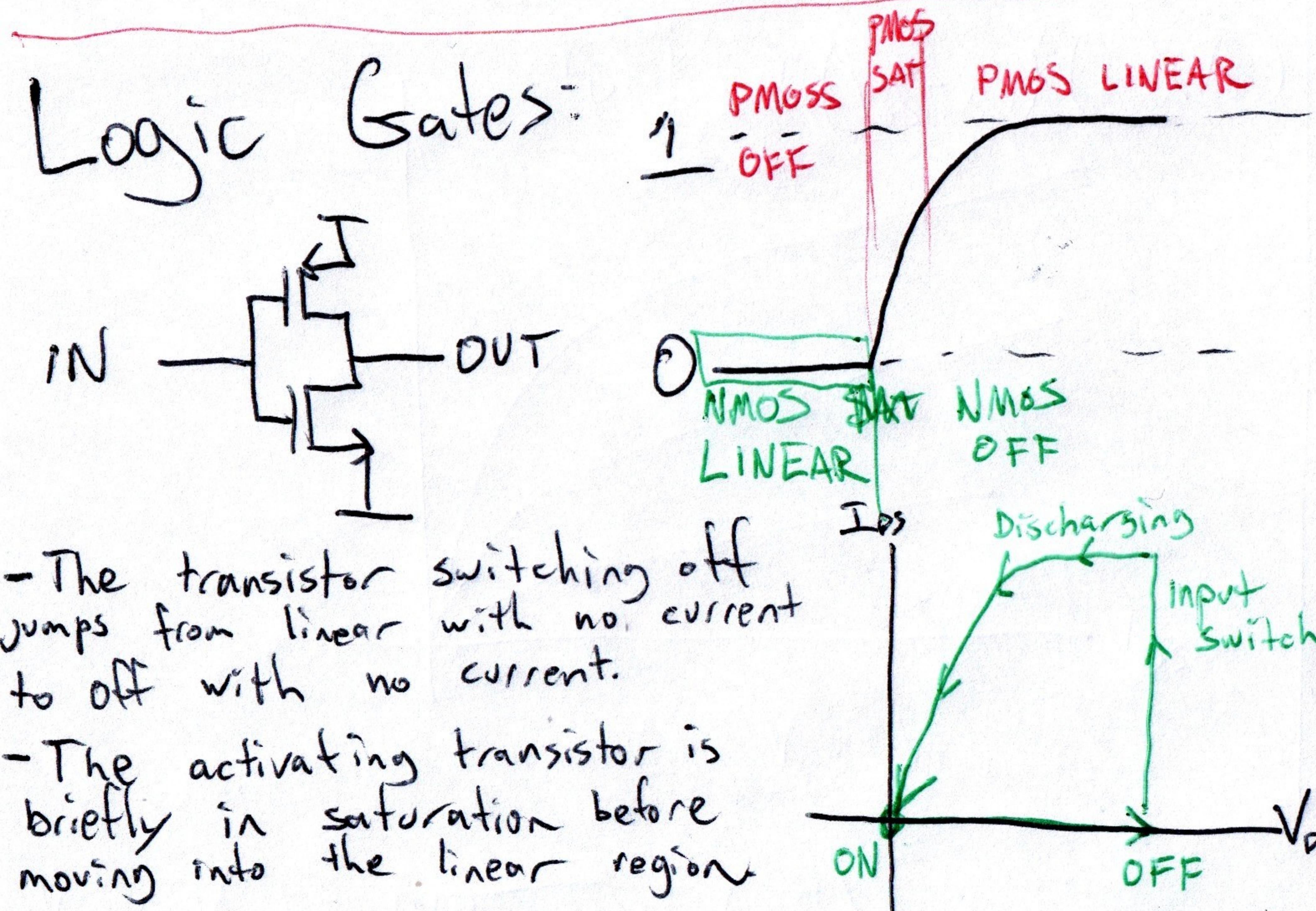
(Do not use any of these in this class)  
(You will only make yourself unhappy.)

# Qualitative Transistor Story Time

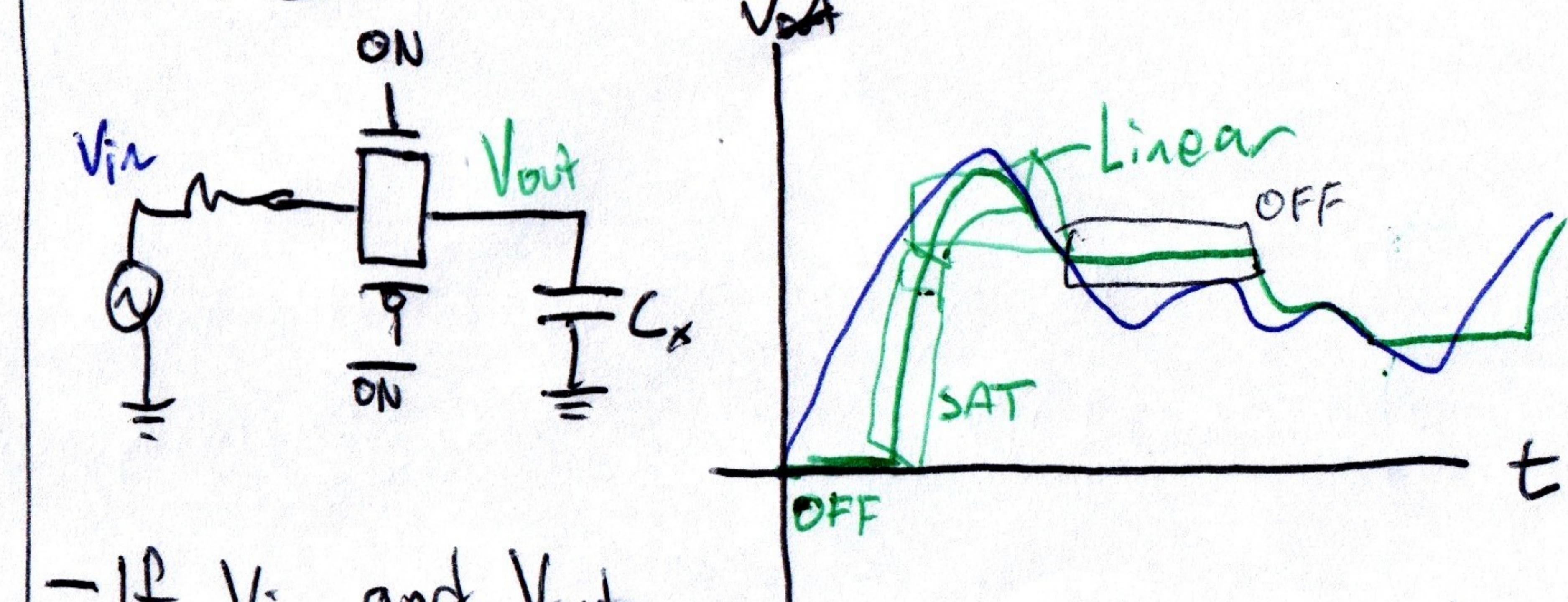
## Amplifiers:



## Logic Gates:



## Analog Switches



- If  $V_{in}$  and  $V_{out}$  are different with the switch on, the devices may be in saturation

- Once  $C_x$  is charged, though, they will be in the linear region

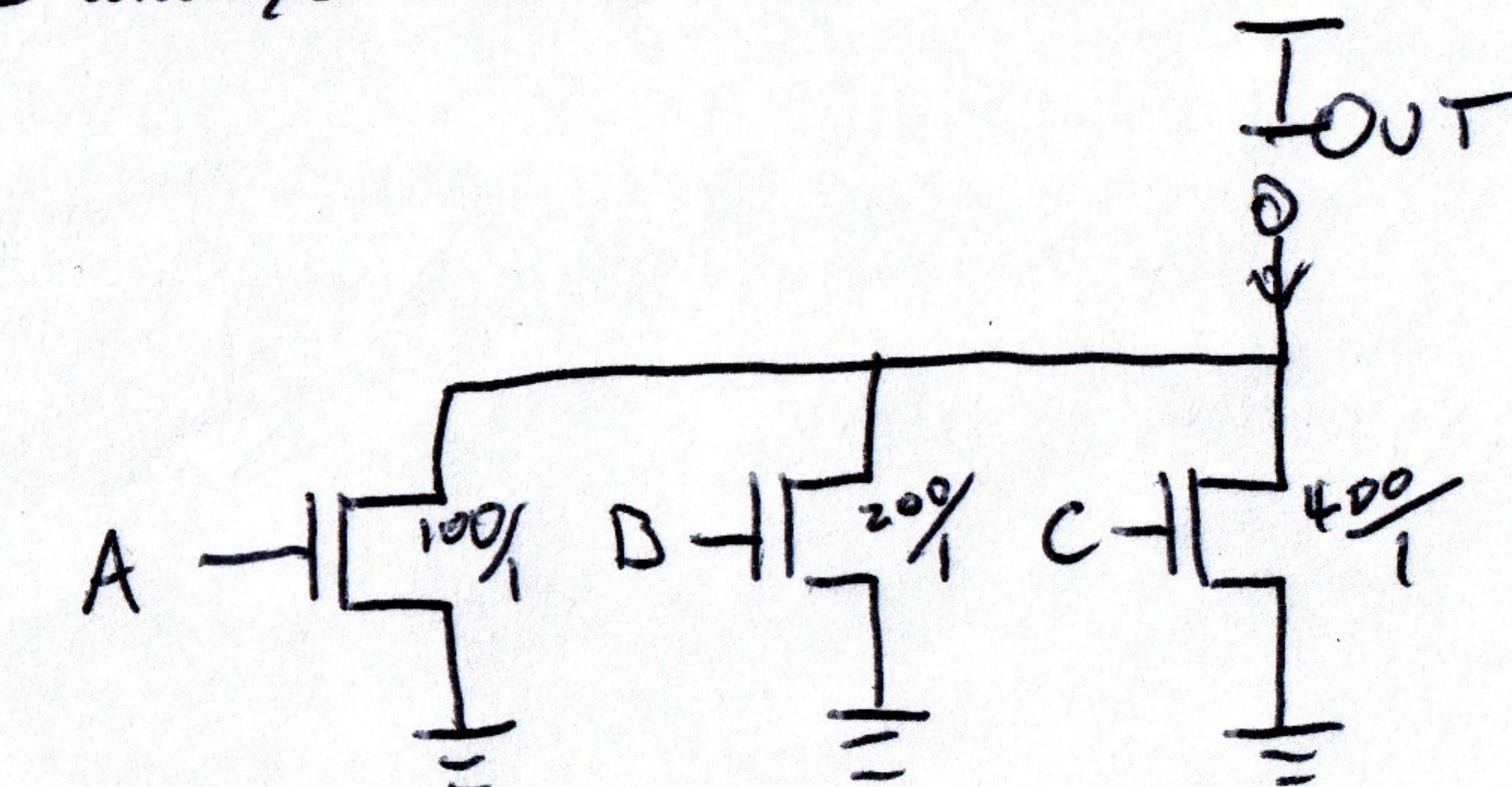
BASICALLY, OFF: any voltage, zero current

SAT: high voltage & current

TRIODE/LINEAR: low voltage & current

## Current-Mode DAC

- The voltage at  $I_{out}$  is always high
- A, B, C always sat or off because of this



| ABC | $I_{out}$ |
|-----|-----------|
| 000 | 0         |
| 100 | 1mA       |
| 110 | 3mA       |
| 001 | 4mA       |
| 101 | 5mA       |